

**Pattern Classification**  
**Homework #2 (Computer Assignment)**

You are given the following sample points in a 2-class problem:

$S_1$ : (1,1), (1,-1), (4,5)

$S_2$ : (2,2), (0,2), (2,3)

Plot them in 2-D feature space. As you can see, they are not linearly separable.

- (a) Are they separable by a higher order polynomial discriminant function? If so, what order do you think is the minimum necessary to separate them (no need to prove. Just explain graphically)?
- (b) Consider the case of a second polynomial discriminant function. Re-pose the problem of finding such a nonlinear discriminant function, as a problem of finding a linear discriminant function for a set of sample points of higher dimension. Give the sample points. Hint:  $\Phi$ -machine
- (c) Using a computer, verify your answers to (a) and (b) by solving for a discriminant function boundary for your linear classifier of part (b); if it doesn't solve, increase order of the polynomial and re-map it to a linear classifier. Verify that your resulting boundary does indeed classify the sample points correctly.  
Hint:
  - A. Use Perceptron.
  - B. To plot the discriminant function, you need to use **solve** and **roots** functions in Matlab.
  - C. To verify the correct classification, plot the boundary and samples in one plot.